

**Bermudian Springs School District
PA Core Standards Math Framework
Seventh Grade – Math and Pre-Algebra**



Introduction

Bermudian Springs School District, in partnership with all stakeholders, recognizes the importance of our students being able to use mathematics in everyday life and in the workplace. New knowledge, tools, and ways of solving math problems will significantly enhance opportunities for shaping our students future. Math competencies open doors to productive futures. All students should have the opportunity and support necessary to learn significant math with depth and understanding. Common Core has provided critical areas designed to bring focus to the standards at each grade by describing key concepts in order to guide instruction. The critical areas for instructional focus for seventh grade math outlined by the *Common Core* include the following four areas:

1. **Developing understanding of and applying proportional relationships.** Students extend their understanding of ratios and develop understanding of proportionality to solve single- and multi-step problems. Students use their understanding of ratios and proportionality to solve a wide variety of percent problems, including those involving discounts, interest, taxes, tips, and percent increase or decrease. Students solve problems about scale drawings by relating corresponding lengths between the objects or by using the fact that relationships of lengths within an object are preserved in similar objects. Students graph proportional relationships and understand the unit rate informally as a measure of the steepness of the related line, called the slope. They distinguish proportional relationships from other relationships.
2. **Developing understanding of operations with rational numbers and working with expressions and linear equations.** Students develop a unified understanding of number, recognizing fractions, decimals (that have a finite or a repeating decimal representation), and percents as different representations of rational numbers. Students extend addition, subtraction, multiplication, and division to all rational numbers, maintaining the properties of operations and the relationships between addition and subtraction, and multiplication and division. By applying these properties, and by viewing negative numbers in terms of everyday contexts (e.g., amounts owed or temperatures below zero), students explain and interpret the rules for adding, subtracting, multiplying, and dividing with negative numbers. They use the arithmetic of rational numbers as they formulate expressions and equations in one variable and use these equations to solve problems.
3. **Solving problems involving scale drawings and informal geometric constructions, and working with two- and three-dimensional shapes to solve problems involving area, surface area, and volume;** Students continue their work with area from Grade 6, solving problems involving the area and circumference of a circle and surface area of three-dimensional objects. In preparation for work on congruence and similarity in Grade 8 they reason about relationships among two-dimensional figures using scale drawings and informal geometric constructions, and they gain familiarity with the relationships between angles formed by intersecting lines. Students work with three-dimensional figures, relating them to two-dimensional figures by examining cross-sections. They solve real-world and mathematical problems involving area, surface area, and volume of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes and right prisms.
4. **Drawing inferences about populations based on samples.** Students build on their previous work with single data distributions to compare two data distributions and address questions about differences between populations. They begin informal work with random sampling to generate data sets and learn about the importance of representative samples for drawing inferences.

Adapted from: PARCC 2013 <http://www.parcconline.org> PDE/SAS 2014

Standards for Mathematical Practice in Seventh Grade

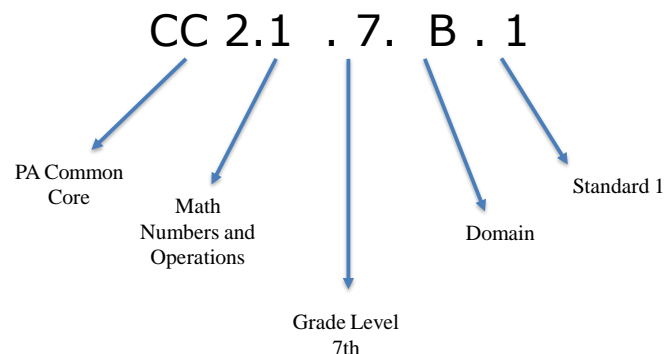
Bermudian Springs School District incorporated the following Mathematical Practices which are expected to be integrated into every mathematics lesson for all students as outlined in the Pennsylvania Core Standards. Below are a few examples of how these mathematical practices may be integrated into some tasks that Bermudian students will apply in seventh grade.

| Standards for Mathematical Practice | Explanations and Examples |
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| 1. Make sense of problems and persevere in solving them. | In grade 7, students solve problems involving ratios and rates and discuss how they solved the problems. Students solve real world problems through the application of algebraic and geometric concepts. Students seek the meaning of a problem and look for efficient ways to represent and solve it. They may check their thinking by asking themselves, “What is the most efficient way to solve the problem?”, “Does this make sense?”, and “Can I solve the problem in a different way?” |
| 2. Reason abstractly and quantitatively. | In grade 7, students represent a wide variety of real world contexts through the use of real numbers and variables in mathematical expressions, equations, and inequalities. Students contextualize to understand the meaning of the number or variable as related to the problem and decontextualize to manipulate symbolic representations by applying properties of operations. |
| 3. Construct viable arguments and critique the reasoning of others. | In grade 7, students construct arguments using verbal or written explanations accompanied by expressions, equations, inequalities, models, and graphs, tables, and other data displays (i.e. box plots, dot plots, histograms, etc.). The students further refine their mathematical communication skills through mathematical discussions in which they critically evaluate their own thinking and the thinking of other students. They pose questions like “How did you get that?”, “Why is that true?” “Does that always work?” They explain their thinking to others and respond to others’ thinking. |
| 4. Model with mathematics. | In grade 7, students model problem situations symbolically, graphically, tabularly, and contextually. Students form expressions, equations, or inequalities from real world contexts and connect symbolic and graphical representations. Students explore covariance and represent two quantities simultaneously. They use measures of center and variability and data displays (i.e. box plots and histograms) to draw inferences, make comparisons and formulate predictions. Students use experiments or simulations to generate data sets and create probability models. Students need many opportunities to connect and explain the connections between the different representations. They should be able to use all of these representations as appropriate to any problem’s context. |
| 5. Use appropriate tools strategically. | Students consider available tools (including estimation and technology) when solving a mathematical problem and decide when certain tools might be helpful. For instance, students in grade 7 may decide to represent similar data sets using dot plots with the same scale to visually compare the center and variability of the data. Students might use physical objects or applets to generate probability data and use graphing calculators or spreadsheets to manage and represent data in different forms. |

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| 6. Attend to precision. | In grade 7, students continue to refine their mathematical communication skills by using clear and precise language in their discussions with others and in their own reasoning. Students define variables, specify units of measure, and label axes accurately. Students use appropriate terminology when referring to rates, ratios, probability models, geometric figures, data displays, and components of expressions, equations or inequalities. |
| 7. Look for and make use of structure. | Students routinely seek patterns or structures to model and solve problems. For instance, students recognize patterns that exist in ratio tables making connections between the constant of proportionality in a table with the slope of a graph. Students apply properties to generate equivalent expressions (i.e. $6 + 2x = 3(2 + x)$ by distributive property) and solve equations (i.e. $2c + 3 = 15$, $2c = 12$ by subtraction property of equality), $c=6$ by division property of equality). Students compose and decompose two- and three-dimensional figures to solve real world problems involving scale drawings, surface area, and volume. Students examine tree diagrams or systematic lists to determine the sample space for compound events and verify that they have listed all possibilities. |
| 8. Look for and express regularity in repeated reasoning. | In grade 7, students use repeated reasoning to understand algorithms and make generalizations about patterns. During multiple opportunities to solve and model problems, they may notice that $a/b \div c/d = ad/bc$ and construct other examples and models that confirm their generalization. They extend their thinking to include complex fractions and rational numbers. Students formally begin to make connections between covariance, rates, and representations showing the relationships between quantities. They create, explain, evaluate, and modify probability models to describe simple and compound events. |

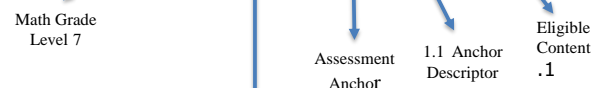
| Mathematical Standards: Development and Progression | | | | | | | | | | | | |
|---|---------------------------------------|---------------------------------------|---|---|---------------------------------------|---|---|---|---|---------------|-------------------------|--|
| | Pre K | K | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | HS | |
| 2.1 Numbers and Operations | (A) Counting & Cardinality | | | | | | | | | | | |
| | | (B) Number and Operations in Base Ten | | | | | | (D) Ratios and Proportional Relationships | | | (F) Number and Quantity | |
| | | | | | (C) Number and Operations - Fractions | | | (E) The Number System | | | | |
| 2.2 Algebraic Concepts | (A) Operations and Algebraic Thinking | | | | | | | (B) Expressions and Equations | | (D) Algebra | | |
| | | | | | | | | | | (C) Functions | | |
| 2.3 Geometry | (A) Geometry | | | | | | | | | | | |
| 2.4 Measurement, Data and Probability | (A) Measurement and Data | | | | | | | (B) Statistics and Probability | | | | |

Standard Taxonomy



Anchor and Eligible Content

M07. C-G.1.1.1



Reporting Categories (different by grade)

- o A-N = The Number System (A – Numbers and
- o B-E = Expressions and Equations
- o B-F = Functions
- o **C-G = Geometry**
- o D-S = Statistics and Probability

2.1 Number and Operations

Domain: (D) Ratios & Proportional Relationships

Standard: CC.2.1.7.D.1 Analyze proportional relationships and use them to model and solve real-world and mathematical problems.

Assessment Anchor: M07.A-R.1.1 Analyze, recognize, and represent proportional relationships and use them to solve real-world and mathematical problems.

- **M07.A-R.1.1.1** Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units. *Example: If a person walks $\frac{1}{2}$ mile in each $\frac{1}{4}$ hour, compute the unit rate as the complex fraction $\frac{1}{2} / \frac{1}{4}$ miles per hour, equivalently 2 miles per hour*
- **M07.A-R.1.1.2** Determine whether two quantities are proportionally related (e.g., by testing for equivalent ratios in a table, or graphing on a coordinate plane and observing whether the graph is a straight line through the origin).
- **M07.A-R.1.1.3** Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships
- **M07.A-R.1.1.4** Represent proportional relationships by equations *Example: If total cost t is proportional to the number n of items purchased at a constant price p , the relationship between the total cost and the number of items can be expressed as $t = p$*
- **M07.A-R.1.1.5** Explain what a point (x, y) on the graph of a proportional relationship means in terms of the situation, with special attention to the points $(0, 0)$ and $(1, r)$ where r is the unit rate
- **M07.A-R.1.1.6** Use proportional relationships to solve multi-step ratio and percent problems *Examples: simple interest, tax, markups and markdowns, gratuities and commissions, fees, percent increase and decrease*

Key Concepts

Key Vocabulary

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| <ul style="list-style-type: none"> • Unit Rates • Proportionality • Percents | unit rate, proportional, constant of proportionality, equations (direct variation), coordinate plane, ratio, percent (related to fractions, decimals), circle graphs, simple interest, tax, markup, markdown, tips, fee, percent increase, percent decrease |
| Competencies <i>Describe what students should be able to do (key skills) as a result of this instruction</i> | |
| <ul style="list-style-type: none"> • Determine unit rates in real world situations • Use proportions to make predictions • Calculate total cost of a grocery bill or dinner out • Calculate population changes • Calculate the height of a structure using similar triangles • Interpret percents and fractions from a circle graph | |

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| 2.1 Number and Operations | |
| Domain: (E) The Number System | |
| Standard: CC.2.1.7.E.1 Apply and extend previous understandings of operations with fractions to operations with rational numbers | |
| Assessment Anchor: M07.A-N.1.1 Solve real-world and mathematical problems involving the four operations with rational numbers. | |
| <ul style="list-style-type: none"> • M07.A-N.1.1.1 Apply properties of operations to add and subtract rational numbers, including real-world contexts. • M07.A-N.1.1.2 Represent addition and subtraction on a horizontal or vertical number line • M07.A-N.1.1.3 Apply properties of operations to multiply and divide rational numbers, including real-world contexts; demonstrate that the decimal form of a rational number terminates or eventually repeats | |
| Key Concepts | Key Vocabulary |
| <ul style="list-style-type: none"> • Integers – add, subtract, multiply, divide • Rational Numbers – add, subtract, multiply, divide | Number line, integer, order of operations, rational number, terminating decimal, repeating decimal, reciprocal |
| Competencies <i>Describe what students should be able to do (key skills) as a result of this instruction</i> | |
| <ul style="list-style-type: none"> • Solve problems using four operations • Represent word problems using the four operations (and any combination of them) | |

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| 2.1 Number and Operations | |
| Domain: (F) Number and Quantity | |
| Standards: CC.2.1.HS.F.1 Apply and extend the properties of exponents to solve problems with rational exponents. CC.2.1.HS.F.2 Apply properties of rational and irrational numbers to solve real world or mathematical problems. | |
| Anchor Descriptor: A1.1.1.1 Represent and/or use numbers in equivalent forms (e.g., integers, fractions, decimals, percents, square roots, and exponents). <ul style="list-style-type: none"> A1.1.1.1.1: Compare and/or order any real numbers. <u>Note:</u> Rational and irrational may be mixed. A1.1.1.1.2: Simplify square roots (e.g., $\sqrt{24} = 2\sqrt{6}$) | |
| Anchor Descriptor: A1.1.1.3 Use exponents, roots, and/or absolute values to solve problems. <ul style="list-style-type: none"> A1.1.1.3.1: Simplify/evaluate expressions involving properties/laws of exponents, roots, and/or absolute values to solve problems. <u>Note:</u> Exponents should be integers from -10 to 10 | |
| Key Concepts | Key Vocabulary <i>* denotes Tier 3 Vocabulary</i> |

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| <ul style="list-style-type: none"> Properties of Rational and Irrational Numbers | Additive Inverse, Composite Number, Estimation Strategy, Exponent, Expression, Irrational Number, Multiplicative Inverse, Negative Exponent, Positive Exponents, Power, Power of a Power, Powers of Products, Radical Expression, Ratio, Commutative Property, Associative Property, Distributive Property, Identity Property, Multiplicative Property of Zero, Cube Root, Integer, Number Line, Order of Operations, Perfect Square, Prime, Number, Rational Number, Repeating Decimal, Square Root, Terminating Decimal, Radical Radicand*, Index* |
| Competencies <i>Describe what students should be able to do (key skills) as a result of this instruction</i> | |
| <ul style="list-style-type: none"> Solve problems working with real number sets (ie; without a calculator, how do we add/subtract the two fractions $\frac{3}{4}$ & $\frac{1}{2}$?) | |

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| 2.1 Number and Operations |
| Domain: (F) Number and Quantity |
| Standard: CC.2.1.HS.F.3 Apply quantitative reasoning to choose and Interpret units and scales in formulas, graphs and data displays. CC.2.1.HS.F.4 Use units as a way to understand problems and to guide the solution of multi-step problems. |
| Anchor Descriptor: A1.1.2.1 Write, solve, and/or graph linear equations using various methods. <ul style="list-style-type: none"> A1.1.2.1.1 Write, solve, and/or apply a linear equation (including problem situations). A1.1.2.1.2 Use and/or identify an algebraic property to justify any step in an equation-solving process. Note: Linear equations only. |
| Anchor Descriptor: A1.1.2.1 Write, solve, and/or graph linear equations using various methods. <ul style="list-style-type: none"> A1.1.2.1.3 Interpret solutions to problems in the context of the problem situation. Note: Linear equations only. |
| Anchor Descriptor: A1.2.1.2 Interpret and/or use linear functions and their equations, graphs, or tables. <ul style="list-style-type: none"> A1.2.1.2.1 Create, interpret, and/or use the equation, graph, or table of a linear function. A1.2.1.2.2 Translate from one representation of a linear function to another (i.e., graph, table, and equation). |

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| Standard: CC.2.1.HS.F.5 Choose a level of accuracy appropriate to limitations on measurement when reporting quantities. | |
| Anchor Descriptor: A1.1.2.1 Write, solve, and/or graph linear equations using various methods. <ul style="list-style-type: none"> A1.1.2.1.1 Write, solve, and/or apply a linear equation (including problem situations). A1.1.2.1.2 Use and/or identify an algebraic property to justify any step in an equation-solving process. Note: Linear equations only. | |
| Anchor Descriptor: A1.1.2.1 Write, solve, and/or graph linear equations using various methods. <ul style="list-style-type: none"> A1.1.2.1.3 Interpret solutions to problems in the context of the problem situation. Note: Linear equations only. | |
| Anchor Descriptor: A1.1.2.2 Write, solve, and/or graph systems of linear equations using various methods. <ul style="list-style-type: none"> A1.1.2.2.1 Write and/or solve a system of linear equations (including problem situations) using graphing, substitution, and/or elimination. Note: Limit systems to two linear equations. A1.1.2.2.2 Interpret solutions to problems in the context of the problem situation. Note: Limit systems to two linear equations. | |
| Anchor Descriptor: A1.1.3.1 Write, solve, and/or graph linear inequalities using various methods. <ul style="list-style-type: none"> A1.1.3.1.1 Write or solve compound inequalities and/or graph their solution sets on a number line (may include absolute value inequalities). A1.1.3.1.2 Identify or graph the solution set to a linear inequality on a number line. A1.1.3.1.3 Interpret solutions to problems in the context of the problem situation. Note: Limit to linear inequalities. | |
| Anchor Descriptor: A1.1.3.2 Write, solve, and/or graph systems of linear inequalities using various methods. <ul style="list-style-type: none"> A1.1.3.2.1 Write and/or solve a system of linear inequalities using graphing. Note: Limit systems to two linear inequalities. A1.1.3.2.2 Interpret solutions to problems in the context of the problem situation. Note: Limit systems to two linear inequalities. | |
| Skills/ Key Concepts | Key Vocabulary |
| <ul style="list-style-type: none"> Solving equations and inequalities | Inequality, equation, solution, inverse operations, one-, two-, multi-step, absolute value equations, inequality, one-, two-, multi-step, compound inequalities, absolute value inequalities |
| Competencies | |
| <i>Describe what students should be able to do (key skills) as a result of this instruction</i> | |
| <ul style="list-style-type: none"> Solve real-world situations described by equations and inequalities using the four operations and inverse operations. | |

2.2 Algebraic Concepts

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| Domain: (B) Expressions and Equations | |
| Standard: CC.2.2.7.B.1 Apply properties of operations to generate equivalent expressions. | |
| Assessment Anchor: M07.B-E.1.1 Use properties of operations to generate equivalent expressions. <ul style="list-style-type: none"> M07.B-E.1.1.1 Apply properties of operations to add, subtract, factor, and expand linear expressions with rational coefficients. <i>Example 1: The expression $\frac{1}{2} \cdot (x + 6)$ is equivalent to $\frac{1}{2} \cdot x + 3$. Example 2: The expression $5.3 - y + 4.2$ is equivalent to $9.5 - y$ (or $-y + 9.5$). Example 3: The expression $4w - 10$ is equivalent to $2(2w - 5)$.</i> | |
| Standard: CC.2.2.7.B.3 Model and solve real- world and mathematical problems by using and connecting numerical, algebraic, and/or graphical representations. | |
| Assessment Anchor: M07.B-E.2.1 Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers. <ul style="list-style-type: none"> M07.B-E.2.1.1 Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate. <i>Example: If a woman making \$25 an hour gets a 10% raise, she will make an additional $\frac{1}{10}$ of her salary an hour, or \$2.50, for a new salary of \$27.50 (or $1.1 \times \\$25 = \\27.50).</i> | |
| Assessment Anchor: M07.B-E.2.2 Use variables to represent quantities in a real-world or mathematical problem, and construct simple equations and inequalities to solve problems. <ul style="list-style-type: none"> M07.B-E.2.2.1 Solve word problems leading to equations of the form $px + q = r$ and $p(x + q) = r$, where p, q, and r are specific rational numbers. <i>Example: The perimeter of a rectangle is 54 cm. Its length is 6 cm. What is its width?</i> M07.B-E.2.2.2 Solve word problems leading to inequalities of the form $px + q > r$ or $px + q < r$, where p, q, and r are specific rational numbers, and graph the solution set of the inequality. <i>Example: A salesperson is paid \$50 per week plus \$3 per sale. This week she wants her pay to be at least \$100. Write an inequality for the number of sales the salesperson needs to make, and describe the solutions</i> | |
| Assessment Anchor: M07.B-E.2.3 Determine the reasonableness of the answer(s) in problem-solving situations. <ul style="list-style-type: none"> M07.B-E.2.3.1 Determine the reasonableness of an answer(s), or interpret the solution(s) in the context of the problem. <i>Example: If you want to place a towel bar that is $9\frac{3}{4}$ inches long in the center of a door that is $27\frac{1}{2}$ inches wide, you will need to place the bar about 9 inches from each edge; this estimate can be used as a check on the exact computation</i> | |
| Key Concepts | Key Vocabulary |
| <ul style="list-style-type: none"> Simplifying expressions Simplifying equations Simplifying inequalities | equivalent expressions, distributive property, combining like terms, coefficient, constant, like terms, one-step equation, two-step equation, multi-step equation, solution, sense, inequality, one-step inequality, two-step inequality |
| Competencies | |
| <i>Describe what students should be able to do (key skills) as a result of this instruction</i> | |
| <ul style="list-style-type: none"> Use distribution and combining like terms to accurately simplify algebraic expressions Use equations and inequalities to represent real-world situations Solve equations based on real-world situations Solve inequalities based on real-world situations | |

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| 2.2 Algebraic Concepts |
| Domain: (C) Functions |
| Standard: CC.2.2.HS.D.7 Create and graph equations or inequalities to describe numbers or relationships. |
| Anchor Descriptor: A1.1.2.1 Write, solve, and/or graph linear equations using various methods. <ul style="list-style-type: none"> A1.1.2.1.1 Write, solve, and/or apply a linear equation (including problem situations). A1.1.2.1.2 Use and/or identify an algebraic property to justify any step in an equation-solving process. Note: Linear equations only. A1.1.2.1.3 Interpret solutions to problems in the context of the problem situation. Note: Linear equations only. |
| Anchor Descriptor: A1.1.3.1 Write, solve, and/or graph linear inequalities using various methods. <ul style="list-style-type: none"> A1.1.3.1.1 Write or solve compound inequalities and/or graph their solution sets on a number line (may include absolute value inequalities). A1.1.3.1.2 Identify or graph the solution set to a linear inequality on a number line. A1.1.3.1.3 Interpret solutions to problems in the context of the problem situation. Note: Limit to linear inequalities. |
| Standard: CC.2.2.HS.D.8 Apply inverse operations to solve equations or formulas for a given variable |
| Anchor Descriptor: A1.1.2.1 Write, solve, and/or graph linear equations using various methods. <ul style="list-style-type: none"> A1.1.2.1.1 Write, solve, and/or apply a linear equation (including problem situations). A1.1.2.1.2 Use and/or identify an algebraic property to justify any step in an equation-solving process. Note: Linear equations only. A1.1.2.1.3 Interpret solutions to problems in the context of the problem situation. Note: Linear equations only. |
| Standard: CC.2.2.HS.D.9 Use reasoning to solve equations and justify the solution method. |
| CC.2.2.HS.D.10 Represent, solve and interpret equations/inequalities and systems of equations/inequalities algebraically and graphically. |
| Anchor Descriptor: A1.1.1.4 Use estimation strategies in problem-solving situations. <ul style="list-style-type: none"> A1.1.1.4.1 Use estimation to solve problems. |
| Anchor Descriptor: A1.1.2.1 Write, solve, and/or graph linear equations using various methods. <ul style="list-style-type: none"> A1.1.2.1.1 Write, solve, and/or apply a linear equation (including problem situations). A1.1.2.1.2 Use and/or identify an algebraic property to justify any step in an equation-solving process. Note: Linear equations only. A1.1.2.1.3 Interpret solutions to problems in the context of the problem situation. Note: Linear equations only. |
| Anchor Descriptor: A1.1.2.2 Write, solve, and/or graph systems of linear equations using various methods. <ul style="list-style-type: none"> A1.1.2.2.1 Write and/or solve a system of linear equations (including problem situations) using graphing, substitution, and/or elimination. Note: Limit systems to two linear equations. A1.1.2.2.2 Interpret solutions to problems in the context of the problem situation. Note: Limit systems to two linear equations. |
| Anchor Descriptor: A1.1.3.1 Write, solve, and/or graph linear inequalities using various methods. <ul style="list-style-type: none"> A1.1.3.1.1 Write or solve compound inequalities and/or graph their solution sets on a number line (may include absolute value inequalities). A1.1.3.1.2 Identify or graph the solution set to a linear inequality on a number line. A1.1.3.1.3 Interpret solutions to problems in the context of the problem situation. Note: Limit to linear inequalities. |
| Standard: CC.2.2.HS.D.10 Represent, solve and interpret equations/inequalities and systems of equations/inequalities algebraically and graphically. |

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| Anchor Descriptor: A1.1.3.2 Write, solve, and/or graph systems of linear inequalities using various methods. <ul style="list-style-type: none"> A1.1.3.2.1 Write and/or solve a system of linear inequalities using graphing. <u>Note:</u> Limit systems to two linear inequalities. A1.1.3.2.2 Interpret solutions to problems in the context of the problem situation. <u>Note:</u> Limit systems to two linear inequalities. | |
| Key Concepts <ul style="list-style-type: none"> Solving equations and inequalities Graphing Linear Equations and Inequalities Solving Linear Systems of Equations and Inequalities Graphing Linear Systems of Equations and Inequalities | Key Vocabulary Equation, Solution, Inverse Operations, One-, Two-, Multi-Step, Absolute Value Equations Inequality, One-, Two-, Multi-Step, Compound Inequalities, Absolute Value Inequalities |
| Competencies <i>Describe what students should be able to do (key skills) as a result of this instruction</i> <ul style="list-style-type: none"> Solve real-world situations described by equations and inequalities using the four operations and inverse operations. | |

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| 2.2 Algebraic Concepts |
| Domain: (C) Functions |
| Standard: CC.2.2.HS.C.1 Use the concept and notation of functions to interpret and apply them in terms of their context. |
| Anchor Descriptor: A1.2.1.1 Analyze and/or use patterns or relations. <ul style="list-style-type: none"> A1.2.1.1.1 Analyze a set of data for the existence of a pattern and represent the pattern algebraically and/or graphically. A1.2.1.1.2 Determine whether a relation is a function, given a set of points or a graph. A1.2.1.1.3 Identify the domain or range of a relation (may be presented as ordered pairs, a graph, or a table). |

Anchor Descriptor: A1.2.2.1 Describe, compute, and/or use the rate of change (slope) of a line.

- **A1.2.2.1.1** Identify, describe, and/or use constant rates of change.
- **A1.2.2.1.2** Apply the concept of linear rate of change (slope) to solve problems.
- **A1.2.2.1.3** Write or identify a linear equation when given the graph of the line, two points on the line, or the slope and a point on the line. Note: Linear equation may be in point-slope, standard, and/or slope-intercept form.
- **A1.2.2.1.4** Determine the slope and/or y-intercept represented by a linear equation or graph.

Standard: CC.2.2.HS.C.2 Graph and analyze functions and use their properties to make connections between the different representations.

Anchor Descriptor: A1.2.1.1 Analyze and/or use patterns or relations.

- **A1.2.1.1.1** Analyze a set of data for the existence of a pattern and represent the pattern algebraically and/or graphically.
- **A1.2.1.1.2** Determine whether a relation is a function, given a set of points or a graph.
- **A1.2.1.1.3** Identify the domain or range of a relation (may be presented as ordered pairs, a graph, or a table).

Anchor Descriptor: A1.2.1.2 Interpret and/or use linear functions and their equations, graphs, or tables.

- **A1.2.1.2.1** Create, interpret, and/or use the equation, graph, or table of a linear function.
- **A1.2.1.2.2** Translate from one representation of a linear function to another (i.e., graph, table, and equation).

Standard: CC.2.2.HS.C.3 Write functions or sequences that model relationships between two quantities.

Anchor Descriptor: A1.1.2.1 Write, solve, and/or graph linear equations using various methods.

- **A1.1.2.1.1** Write, solve, and/or apply a linear equation (including problem situations).
- **A1.1.2.1.2** Use and/or identify an algebraic property to justify any step in an equation-solving process. Note: Linear equations only.
- **A1.1.2.1.3** Interpret solutions to problems in the context of the problem situation. Note: Linear equations only.

Anchor Descriptor: A1.2.1.1 Analyze and/or use patterns or relations.

- **A1.2.1.1.1** Analyze a set of data for the existence of a pattern and represent the pattern algebraically and/or graphically.
- **A1.2.1.1.2** Determine whether a relation is a function, given a set of points or a graph.
- **A1.2.1.1.3** Identify the domain or range of a relation (may be presented as ordered pairs, a graph, or a table).

Anchor Descriptor: A1.2.1.2 Interpret and/or use linear functions and their equations, graphs, or tables.

- **A1.2.1.2.1** Create, interpret, and/or use the equation, graph, or table of a linear function.
- **A1.2.1.2.2** Translate from one representation of a linear function to another (i.e., graph, table, and equation).

Anchor Descriptor: A1.2.2.1 Describe, compute, and/or use the rate of change (slope) of a line.

- **A1.2.2.1.1** Identify, describe, and/or use constant rates of change.
- **A1.2.2.1.2** Apply the concept of linear rate of change (slope) to solve problems.
- **A1.2.2.1.3** Write or identify a linear equation when given the graph of the line, two points on the line, or the slope and a point on the line. Note: Linear equation may be in point-slope, standard, and/or slope-intercept form.
- **A1.2.2.1.4** Determine the slope and/or y-intercept represented by a linear equation or graph.

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| Standard: CC.2.2.HS.C.4 Interpret the effects transformations have on functions and find the inverses of functions. | |
| Anchor Descriptor: A1.2.1.2 Interpret and/or use linear functions and their equations, graphs, or tables. <ul style="list-style-type: none"> A1.2.1.2.1 Create, interpret, and/or use the equation, graph, or table of a linear function. A1.2.1.2.2 Translate from one representation of a linear function to another (i.e., graph, table, and equation). | |
| Standard: CC.2.2.HS.C.5 Construct and compare linear, quadratic and exponential models to solve problems. | |
| Anchor Descriptor: A1.2.2.1 Describe, compute, and/or use the rate of change (slope) of a line. <ul style="list-style-type: none"> A1.2.2.1.1 Identify, describe, and/or use constant rates of change. A1.2.2.1.2 Apply the concept of linear rate of change (slope) to solve problems. | |
| Anchor Descriptor: A1.2.2.1 Describe, compute, and/or use the rate of change (slope) of a line. <ul style="list-style-type: none"> A1.2.2.1.3 Write or identify a linear equation when given the graph of the line, two points on the line, or the slope and a point on the line. Note: Linear equation may be in point-slope, standard, and/or slope-intercept form. A1.2.2.1.4 Determine the slope and/or y-intercept represented by a linear equation or graph. | |
| Standard: CC.2.2.HS.C.6 Interpret functions in terms of the situation they model. | |
| Anchor Descriptor: A1.2.1.2 Interpret and/or use linear functions and their equations, graphs, or tables. <ul style="list-style-type: none"> A1.2.1.2.1 Create, interpret, and/or use the equation, graph, or table of a linear function. A1.2.1.2.2 Translate from one representation of a linear function to another (i.e., graph, table, and equation). | |
| Anchor Descriptor: A1.2.2.2 Analyze and/or interpret data on a scatter plot. <ul style="list-style-type: none"> A1.2.2.2.1 Draw, identify, find, and/or write an equation for a line of best fit for a scatter plot. | |
| Key Concepts | Key Vocabulary |
| <ul style="list-style-type: none"> Relations Functions | sketch, continuous, discrete, function, relation, vertical line test, function notation, domain, range, input, output, dependent variable, independent variable, linear function, nonlinear function, quadratic equation, absolute value equation |
| Competencies <i>Describe what students should be able to do (key skills) as a result of this instruction</i> | |

- Solve real-world problems using function notation
- Describe a logical argument to describe if different representations of relations are or are not functions (ie; mapping, ordered pairs, table of values, graphical illustration, etc.)
- Create original sketches to describe functions (linear, nonlinear, quadratic and absolute value) that are continuous and discrete
Find a function's output/range when given the input/domain values

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| Domain: (A) Geometry | |
| Standard: CC.2.3.7.A.1 Solve real-world and mathematical problems involving angle measure, area, surface area, circumference, and volume. | |
| Assessment Anchor: M07.C-G.2.1 Identify, use and describe properties of angles and their measures. <ul style="list-style-type: none"> • M07.C-G.2.1.1 Identify and use properties of supplementary, complementary, and adjacent angles in a multistep problem to write and solve simple equations for an unknown angle in a figure • M07.C-G.2.1.2 Identify and use properties of angles formed when two parallel lines are cut by a transversal (e.g., angles may include alternate interior, alternate exterior, vertical, corresponding). | |
| Assessment Anchor: M07.C-G.2.2 Determine circumference, area, surface area, and volume. <ul style="list-style-type: none"> • M07.C-G.2.2.1 Find the area and circumference of a circle. Solve problems involving area and circumference of a circle(s). Formulas will be provided • M07.C-G.2.2.2 Solve real-world and mathematical problems involving area, volume, and surface area of two-and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms. Formulas will be provided | |
| Standard: CC.2.3.7.A.2 Visualize and represent geometric figures and describe the relationships between them. | |
| Assessment Anchor: M07.C-G.1.1 Describe and apply properties of geometric figures. <ul style="list-style-type: none"> • M07.C-G.1.1.1 Solve problems involving scale drawings of geometric figures, including finding length and area. • M07.C-G.1.1.2 Identify or describe the properties of all types of triangles based on angle and side measure • M07.C-G.1.1.3 Use and apply the triangle inequality theorem • M07.C-G.1.1.4 Describe the two-dimensional figures that result from slicing three-dimensional figures | |
| Key Concepts | Key Vocabulary |
| <ul style="list-style-type: none"> • Angle measures • Two- and three-dimensional objects • Triangles | supplementary, complimentary, adjacent, parallel lines, transversal, alternate interior, alternate exterior, vertical, corresponding, cross-section, area, circumference, volume, surface area, quadrilateral, polygon, right prism, properties, triangle, inequality theorem |
| Competencies | |
| <i>Describe what students should be able to do (key skills) as a result of this instruction</i> | |
| <ul style="list-style-type: none"> • Identify the relationship between different angle measures • Calculate angle measures given enough appropriate information • Use formulas to calculate area, volume, and surface area • Relate triangles | |

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| 2.4 Measurement, Data and Probability | |
| Domain: (B) Statistics and Probability | |
| Standard: CC.2.4.7.B.1 Draw inferences about populations based on random sampling concepts. | |
| Assessment Anchor: M07.C-G.2.2 Determine circumference, area, surface area, and volume. <ul style="list-style-type: none"> • M07.D-S.1.1.1 Determine whether a sample is a random sample given a real-world situation • M07.D-S.1.1.2 Use data from a random sample to draw inferences about a population with an unknown characteristic of interest <i>Example 1: Estimate the mean word length in a book by randomly sampling words from the book Example 2: Predict the winner of a school election based on randomly sampled survey data.</i> | |
| Standard: CC.2.4.7.B.2 Draw informal comparative inferences about two populations. | |
| Assessment Anchor: M07.D-S.2.1 Use statistical measures to compare two numerical data distributions. <ul style="list-style-type: none"> • M07.D-S.2.1.1 Compare two numerical data distributions using measures of center and variability. <i>Example 1: The mean height of players on the basketball team is 10 cm greater than the mean height of players on the soccer team. This difference is equal to approximately twice the variability (mean absolute deviation) on either team. On a line plot, note the difference between the two distributions of heights. Example 2: Decide whether the words in a chapter of a seventh-grade science book are generally longer than the words in a chapter of a fourth-grade science book</i> | |
| Standard: CC.2.4.7.B.3 Investigate chance processes and develop, use, and evaluate probability models. | |
| Assessment Anchor: M07.D-S.3.1 Predict or determine the likelihood of outcomes. <ul style="list-style-type: none"> • M07.D-S.3.1.1 Predict or determine whether some outcomes are certain, more likely, less likely, equally likely, or impossible. (i.e., a probability near 0 indicates an unlikely event, a probability around 1/2 indicates an event that is neither unlikely nor likely, and a probability near 1 indicates a likely event) | |
| Assessment Anchor: M07.D-S.3.2 Use probability to predict outcomes. <ul style="list-style-type: none"> • M07.D-S.3.2.1 Determine the probability of a chance event given relative frequency. Predict the approximate relative frequency given the probability. <i>Example: When rolling a number cube 600 times, predict that a 3 or 6 would be rolled roughly 200 times, but probably not exactly 200 times</i> • M07.D-S.3.2.2 Find the probability of a simple event, including the probability of a simple event not occurring. <i>Example: What is the probability of not rolling a 1 on a number cube?</i> • M07.D-S.3.2.3 Find probabilities of independent compound events using organized lists, tables, tree diagrams, and simulation. | |
| Key Concepts | Key Vocabulary |
| <ul style="list-style-type: none"> • Sampling • Measures of central tendency • Measure of dispersion • Probability | random, stratified, systematic, mean, median, mode, range, absolute deviation, (line plot, stem-and-leaf warm-ups), spectrum, predictions, simple events (not), compound events, independent events, (dependent events to help out Alg 1A?) |

Competencies

Describe what students should be able to do (key skills) as a result of this instruction

- Identify the different types of sampling and when one is a better option than the other
- Create, conduct, and interpret survey data
- Compare data sets using measures of central tendency and dispersion
- Calculate probability of simple and compound events including using it to make predictions

2.4 Measurement, Data and Probability

Domain: (B) Statistics and Probability

Standard: CC.2.4.HS.B.1 Summarize, represent, and interpret data on a single count or measurement variable.

CC.2.4.HS.B.3 Analyze linear models to make interpretations based on the data.

Anchor Descriptor: A.1.2.3.1 Use measures of dispersion to describe a set of data.

- A1.2.3.1.1 Calculate and/or interpret the range, quartiles, and interquartile range of data.

Anchor Descriptor: A.1.2.3.2 Use data displays in problem-solving setting and/or to make predictions.

- A1.2.3.2.1 Estimate or calculate to make predictions based on a circle, line, bar graph, measures of central tendency, or other representations.
- A1.2.3.2.2 Analyze data, make predictions, and/or answer questions based on displayed data.
- A1.2.3.2.3 Make predictions using the equations or graphs of best-fit lines of scatter plots.

Standard: CC.2.4.HS.B.3 Analyze linear models to make interpretations based on the data.

Anchor Descriptor: A.1.2.2.2 Analyze and/or interpret data on a scatter plot.

- A1.2.2.2.1 Draw, identify, find, and/or write an equation for a line of best fit for a scatter plot.

Standard: CC.2.4.HS.B.4 Recognize and evaluate random processes underlying statistical experiments.

CC.2.4.HS.B.7 Apply the rules of probability to compute probabilities of compound events in a uniform probability model.

Anchor Descriptor: A1.2.3.3 Apply probability to practical situations.

- A1.2.3.3.1 Find probabilities for compound events (e.g., find probability of red and blue, find probability of red or blue) and represent as a fraction, decimal, or percent.

Standard: CC.2.4.HS.B.5 Make inferences and justify conclusions based on sample surveys, experiments, and observational studies.

Anchor Descriptor: A.1.2.3.2 Use data displays in problem-solving setting and/or to make predictions.

- **A1.2.3.2.1** Estimate or calculate to make predictions based on a circle, line, bar graph, measures of central tendency, or other representations.
- **A1.2.3.2.2** Analyze data, make predictions, and/or answer questions based on displayed data.
- **A1.2.3.2.3** Make predictions using the equations or graphs of best-fit lines of scatter plots.

Key Concepts

- Measures of central tendency and dispersion
- Box-and-whisker plots
- Samples and surveys
- Probability
- Displaying and representing data

Key Vocabulary

measures of central tendency, mean, median, mode, measure of dispersion, range, outlier, absolute deviation, minimum, maximum, quartile 1 (lower quartile), quartile 3 (upper quartile), interquartile range, random, stratified, bivariate, univariate, qualitative, quantitative, probability, theoretical, experimental, outcome, event, sample space, compound event, independent event, dependent event, overlapping, vent, mutually exclusive, multiple line/bar graphs, line plot

Competencies

Describe what students should be able to do (key skills) as a result of this instruction

- Determine a data set's mean, median, mode, and range
- From a given data set, identify the parts of a box-and-whisker plot (minimum, Q1, median, Q3, maximum values)
- Make applications from a box-and-whisker plot representation: identify the parts (minimum, Q1, median, Q3, maximum values)
- Interpret and analyze data given in different graphical representations
- Collect, organize, and analyze data from experiments (samples and surveys)
Solve real-world problems involving different types of probabilities (ie; the chance of rolling an odd number on a regular 6-sided dice or spinning a 2 on a spinner that is separated into 8 equal, numbered sections)